

DSSP

Table Wrangling & Data Visualization

A. Bichat - E. Le Pennec



2019 - 2020



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

Anscombe Quartet

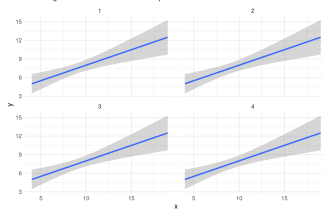
	x1	y1	x2	y2	x3	y3	x4	y4
1	10	8.04	10	9.14	10	7.46	8	6.58
2	8	6.95	8	8.14	8	6.77	8	5.76
3	13	7.58	13	8.74	13	12.74	8	7.71
4	9	8.81	9	8.77	9	7.11	8	8.84
5	11	8.33	11	9.26	11	7.81	8	8.47
6	14	9.96	14	8.1	14	8.84	8	7.04
7	6	7.24	6	6.13	6	6.08	8	5.25
8	4	4.26	4	3.1	4	5.39	19	12.5
9	12	10.84	12	9.13	12	8.15	8	5.56
10	7	4.82	7	7.26	7	6.42	8	7.91
11	5	5.68	5	4.74	5	5.73	8	6.89

From

to

Anscombe Quartet

Linear regression with confidence bar and points



From Table to Graph

- Need to manipulate tables.
- Need to visualize tables.

Outline



- 1 Introduction
- 2 Table Wrangling**
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle



Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

- Each observation forms a row.

Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

- Each observation forms a row.
- Each variable forms a column.



Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

- Each observation forms a row.
- Each variable forms a column.

- Columns are named, rows are not.
- Columns made of values of the same type.



Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

- Each observation forms a row.
 - Each variable forms a column.
 - Each type of observational unit forms a table.
-
- Columns are named, rows are not.
 - Columns made of values of the same type.
 - Codd's 3rd normal form...



Tidy Table

a	b	c	d
5			A
1			B
4			A
5			B
2			B

- Each observation forms a row.
- Each variable forms a column.
- Each type of observational unit forms a table.

- Columns are named, rows are not.
- Columns made of values of the same type.
- Codd's 3rd normal form...

In practice

- Definition of observation may depend on the task.
- Tidying data is a real work!



	a	b	c	d
5				A
1				B
4				A
5				B
2				B

Verbs

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
4			A

Filter

Verbs

- Rows: Filter,

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	d
5	A
1	B
4	A
5	B
2	B

Select

Verbs

- Rows: Filter,
- Columns: Remove,

Table Actions



a	b	c	d
5			A
1			B
4			A
5			B
2			B
3			A

Insert

a	b	c	d
5			A
1			B
4			A
5			B
2			B

Verbs

- Rows: Filter, Insert
- Columns: Remove,



	a	b	c	d
5				A
1				B
4				A
5				B
2				B

	a	b	c	d	e
5				A	10
1				B	2
4				A	8
5				B	10
2				B	4

Add

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add



a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d	e
5			A	10
1			B	2
4			A	8
5			B	10
2			B	4

Transform

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, ,



a'
17
Summarize

a	b	c	d
5			A
1			B
4			A
5			B
2			B

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize,



	a	b	c	d
5				A
1				B
4				A
5				B
2				B

	a	b	c	d
1				B
2				B
4				A
5				A
5				B

Sort

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort



a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split

d	a'
A	9
B	8

d	a'
A	9
B	8

Split/Apply/Combine

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split/Apply/Combine (Summarize)

Table Actions



a'

17

Summarize

a	b	c	d
5			A
1			B
4			A
5			B
2			B
3			A

Insert

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
4			A

Filter

a	b	c	d	e
5			A	10
1			B	2
4			A	8
5			B	10
2			B	4

Add/Transform

a	d
5	A
1	B
4	A
5	B
2	B

Select

a	b	c	d
1			B
2			B
4			A
5			A
5			B

Sort

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split

d	a'
A	9
B	8

Split/Apply/Combine

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split/Apply/Combine (Summarize)

Table Actions



a'

17

Summarize
SELECT

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
1			B
4			A
5			B
2			B
3			A

Insert
INSERT/UNION

a	b	c	d
5			A
4			A

Filter
WHERE

a	b	c	d	e
5			A	10
1			B	2
4			A	8
5			B	10
2			B	4

Add/Transform
SELECT

a	d
5	A
1	B
4	A
5	B
2	B

Select
SELECT

a	b	c	d
1			B
2			B
4			A
5			A
5			B

Sort
ORDER BY

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split
GROUP BY

d	a'
A	9
B	8

Split/Apply/Combine
SELECT + GROUP BY

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split/Apply/Combine (Summarize)

Table Actions



a'

17

Summarize
summarize

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
1			B
4			A
5			B
2			B
3			A

Insert
bind_rows
a b c d

5			A
4			A

Filter
filter

a	b	c	d	e
5			A	10
1			B	2
4			A	8
5			B	10
2			B	4

Add/Transform
bind_cols/mutate

a	d
5	A
1	B
4	A
5	B
2	B

Select
select

a	b	c	d
1			B
2			B
4			A
5			A
5			B

Sort
arrange

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split
group_by

d	a'
A	9
B	8

Split/Apply/Combine
group_by + summarize

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split/Apply/Combine (Summarize)

Table Actions



a'

17

Summarize
agg

a	b	c	d
5			A
1			B
4			A
5			B
2			B

a	b	c	d
5			A
1			B
4			A
5			B
2			B
3			A

Insert
concat

a	b	c	d
5			A
4			A

Filter
query

a	b	c	d	e
5			A	10
1			B	2
4			A	8
5			B	10
2			B	4

Add/Transform
assign

a	d
5	A
1	B
4	A
5	B
2	B

Select
loc

a	b	c	d
1			B
2			B
4			A
5			A
5			B

Sort
sort_values

a	b	c	d
5			A
4			A
1			B
5			B
2			B

Split
groupby

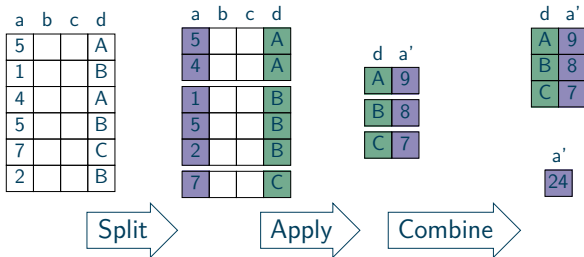
d	a'
A	9
B	8

Split/Apply/Combine
groupby + agg

Verbs

- Rows: Filter, Insert
- Columns: Remove, Add
- Rows/Columns: Transform, Summarize, Sort
- Split/Apply/Combine (Summarize)

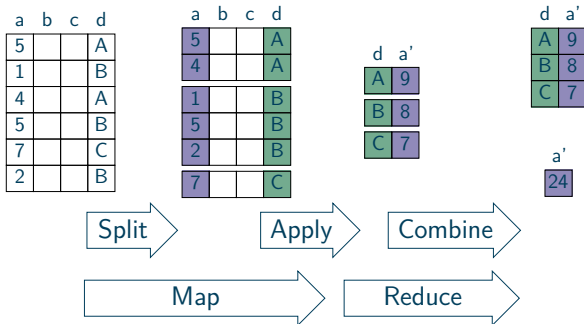
Split/Apply/Combine



Split/Apply/Combine

- **Split** the data by some **grouping** variable
- **Apply** some function to each group independently
- **Combine** the data into some **output**.

Split/Apply/Combine



Split/Apply/Combine

- **Split** the data by some **grouping** variable
 - **Apply** some function to each group independently
 - **Combine** the data into some **output**.
-
- **Map/Reduce** ~ **Split/Apply/Combine**.

Joining Two Tables



	d	k	e
1	A		
2	B		
3	A		
4	D		

	a	b	c	k
1				A
2				B
3				A
4				C
5				B

Join between two tables along a key

Joining Two Tables

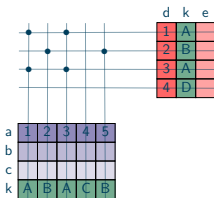


	d	k	e
1	A		
2	B		
3	A		
4	D		

a	1	2	3	4	5
b					
c					
k	A	B	A	C	B

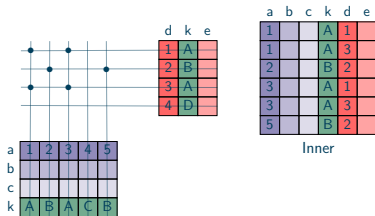
Join between two tables along a key

Joining Two Tables



Join between two tables along a key

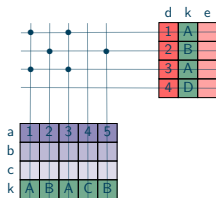
Joining Two Tables



Join between two tables along a key

- Inner

Joining Two Tables



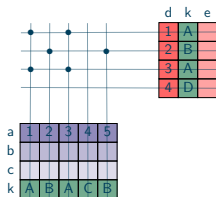
	a	b	c	k	d	e
1				A	1	
1				A	3	
2				B	2	
3				A	1	
3				A	3	
4				C	?	?
5				B	2	

Left

Join between two tables along a key

- Inner
- Outer: left

Joining Two Tables



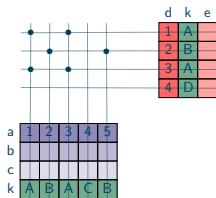
a	b	c	k	d	e
1			A	1	
3			A	1	
2			B	2	
5			B	2	
1			A	3	
3			A	3	
?	?	?	D	4	

Right

Join between two tables along a key

- Inner
- Outer: left, right

Joining Two Tables



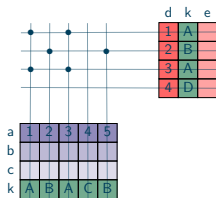
	a	b	c	k	d	e
1				A	1	
2				B	3	
3				A	1	
4				A	3	
5				C	?	?
?		?	?	D	4	

Full

Join between two tables along a key

- Inner
- Outer: left, right, full

Joining Two Tables



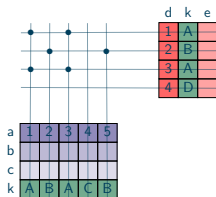
a	b	c	k
1			A
2			B
3			A
5			B

Semi

Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi

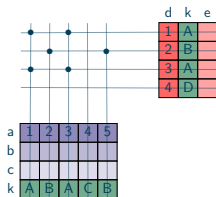
Joining Two Tables



Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi, anti

Joining Two Tables



	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	5			B	2	

Inner

	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	4			C	?	?
7	5			B	2	

Left

	a	b	c	k	d	e
1	1			A	1	
2	3			A	1	
3	2			B	2	
4	5			B	2	
5	1			A	3	
6	3			A	3	
7	?	?	?	D	4	

Right

	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	4			C	?	?
7	5			B	2	
8	?	?	?	D	4	

Full

	a	b	c	k
1	1			A
2	2			B
3	3			A
4	5			B

Semi

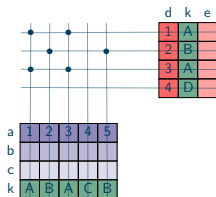
	a	b	c	k
4				C

Anti

Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi, anti

Joining Two Tables



	a	b	c	k	d	e
1				A	1	
1				A	3	
2				B	2	
3				A	1	
3				A	3	
5				B	2	

Inner JOIN

	a	b	c	k	d	e
1				A	1	
1				A	3	
2				B	2	
3				A	1	
3				A	3	
4				C	?	?
5				B	2	

Left LEFT JOIN

	a	b	c	k	d	e
1				A	1	
3				A	1	
2				B	2	
5				B	2	
1				A	3	
3				A	3	
?	?	?	?	D	4	

Right RIGHT JOIN

	a	b	c	k	d	e
1				A	1	
1				A	3	
2				B	2	
3				A	1	
3				A	3	
4				C	?	?
5				B	2	
?	?	?	?	D	4	

Full FULL JOIN

	a	b	c	k
1				A
2				B
3				A
5				B

Semi SEMI JOIN

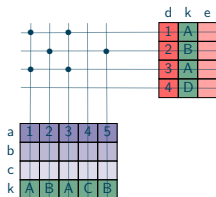
	a	b	c	k
4				C

Anti ANTI JOIN

Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi, anti

Joining Two Tables



	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	5			B	2	

Inner
inner_join

	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	4			C	?	?
7	5			B	2	

Left
left_join

	a	b	c	k	d	e
1	1			A	1	
2	3			A	1	
3	2			B	2	
4	5			B	2	
5	1			A	3	
6	3			A	3	
7	?	?	?	D	4	

Right
right_join

	a	b	c	k	d	e
1	1			A	1	
2	1			A	3	
3	2			B	2	
4	3			A	1	
5	3			A	3	
6	4			C	?	?
7	5			B	2	
8	?	?	?	D	4	

Full
full_join

	a	b	c	k
1	1			A
2	2			B
3	3			A
4	5			B

Semi
semi_join

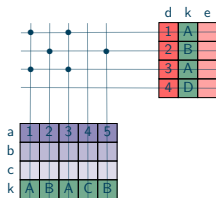
	a	b	c	k
4				C

Anti
anti_join

Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi, anti

Joining Two Tables



a	b	c	k	d	e
1			A	1	
1			A	3	
2			B	2	
3			A	1	
3			A	3	
5			B	2	

Inner
merge (inner)

a	b	c	k	d	e
1			A	1	
1			A	3	
2			B	2	
3			A	1	
3			A	3	
4			C	?	?
5			B	2	

Left
merge (left)

a	b	c	k	d	e
1			A	1	
3			A	1	
2			B	2	
5			B	2	
1			A	3	
3			A	3	
?	?	?	D	4	

Right
merge (right)

a	b	c	k	d	e
1			A	1	
1			A	3	
2			B	2	
3			A	1	
3			A	3	
4			C	?	?
5			B	2	
?	?	?	D	4	

Full
merge (full)

a	b	c	k
1			A
2			B
3			A
5			B

Semi
merge (inner) + loc

a	b	c	k
4			C

Anti
merge (inner) + loc

Join between two tables along a key

- Inner
- Outer: left, right, full
- Other: semi, anti



	a	b	c	d	e
E	A	5			
E	B	1			
F	A	4			
F	B	5			
G	C	7			
G	B	2			

- Several ways to organize information.

Table Reshaping

	a	b	c	d	e
E	A	5			
E	B	1			
F	A	4			
F	B	5			
G	C	7			
G	B	2			



a	A	B	C
E	5	1	?
F	5	5	?
G	?	2	7

- Several ways to organize information.

Table Reshaping

- Pivot: Categories to columns

	a	b	c	d	e
E	A	5			
E	B	1			
F	A	4			
F	B	5			
G	C	7			
G	B	2			

Pivot

a	A	B	C
E	5	1	?
F	5	5	?
G	?	2	7

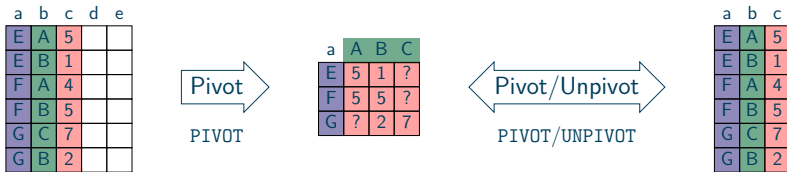
Pivot/Unpivot

	a	b	c
E	A	5	
E	B	1	
F	A	4	
F	B <td>5</td> <td></td>	5	
G	C	7	
G	B	2	

- Several ways to organize information.

Table Reshaping

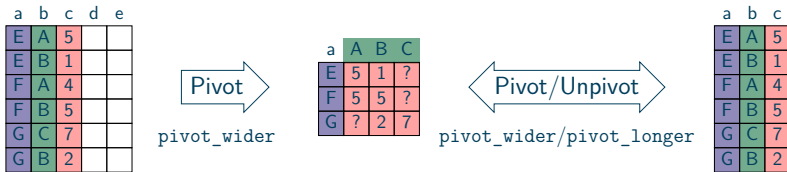
- Pivot: Categories to columns
- Unpivot: Columns to categories



- Several ways to organize information.

Table Reshaping

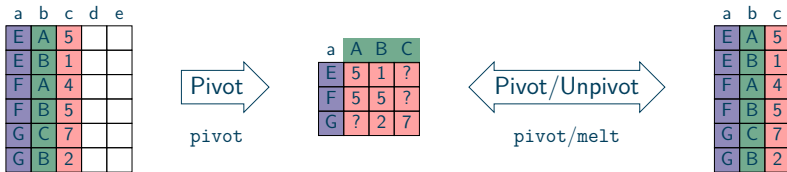
- Pivot: Categories to columns
- Unpivot: Columns to categories



- Several ways to organize information.

Table Reshaping

- Pivot: Categories to columns
- Unpivot: Columns to categories



- Several ways to organize information.

Table Reshaping

- Pivot: Categories to columns
- Unpivot: Columns to categories

	a	b	c	d	e
E	A	5			
E	B	1			
F	A	4			
F	B	5			
G	C	7			
G	B	2			

Pivot

Wide

a	A	B	C
E	5	1	?
F	5	5	?
G	?	2	7

Pivot/Unpivot

Long

a	b	c
E	A	5
E	B	1
F	A	4
F	B	5
G	C	7
G	B	2

- Several ways to organize information.

Table Reshaping

- Pivot: Categories to columns
- Unpivot: Columns to categories

- Wide / Long format

	a	b	c	d	e
E	A	5			
E	B	1			
F	A	4			
F	B	5			
G	C	7			
G	B	2			

Pivot

a	A	B	C
E	5	1	?
F	5	5	?
G	?	2	7

Pivot/Unpivot

	a	b	c
E	A	5	
E	B	1	
F	A	4	
F	B	5	
G	C	7	
G	B	2	

- Several ways to organize information.

Table Reshaping

- Pivot: Categories to columns
- Unpivot: Columns to categories

- Best format depends on the task



Local Files: CSV, JSON, xls,...

- Dedicated import(/export) libraries
- Often weakly typed.
- Cleaning often required.
- Typed variants exists: arrow, feather...

Database: SQL, NoSQL,...

- Dedicated DB connectors.
- SQL as a common language.
- Often already cleaned.
- Local files may be accessed through a DB interface...

Web: HTML

- Web scraping library
- Often a lot of cleaning
- Web API ~ Local files...



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization**
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization**
 - **Introduction**
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

Why Data Visualization?



Data visualization can:

- provide a clear understanding of patterns in data
- detect hidden structures in data
- condense information



Data visualization can:

- provide a clear understanding of patterns in data
 - detect hidden structures in data
 - condense information
-
- Anscombe's quartet example:

Anscombe Quartet

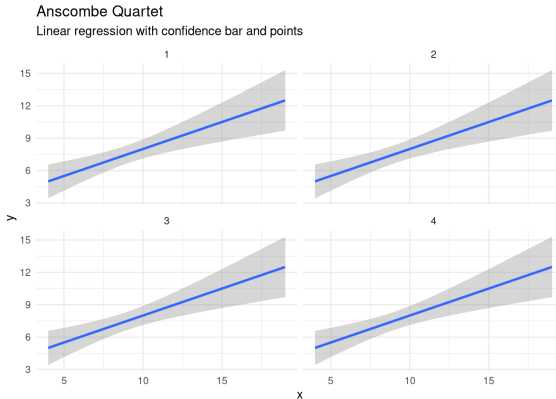
	x1	y1	x2	y2	x3	y3	x4	y4
1	10	8.04	10	9.14	10	7.46	8	6.58
2	8	6.95	8	8.14	8	6.77	8	5.76
3	13	7.58	13	8.74	13	12.74	8	7.71
4	9	8.81	9	8.77	9	7.11	8	8.84
5	11	8.33	11	9.26	11	7.81	8	8.47
6	14	9.96	14	8.1	14	8.84	8	7.04
7	6	7.24	6	6.13	6	6.08	8	5.25
8	4	4.26	4	3.1	4	5.39	19	12.5
9	12	10.84	12	9.13	12	8.15	8	5.56
10	7	4.82	7	7.26	7	6.42	8	7.91
11	5	5.68	5	4.74	5	5.73	8	6.89

Why Data Visualization?



Data visualization can:

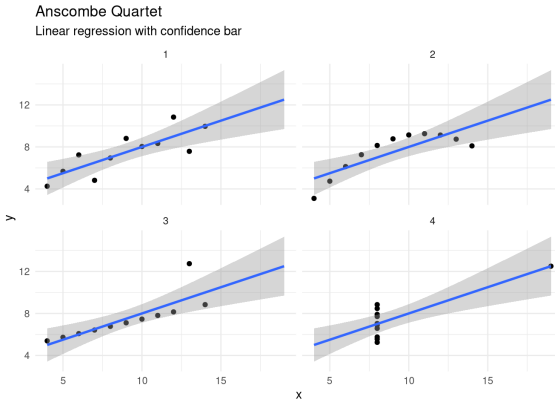
- provide a clear understanding of patterns in data
 - detect hidden structures in data
 - condense information
-
- Anscombe's quartet example:



Why Data Visualization?

Data visualization can:

- provide a clear understanding of patterns in data
 - detect hidden structures in data
 - condense information
-
- Anscombe's quartet example:





Focus of today

- Standard data visualization techniques,
- Review of various graphical techniques,
- Principle of good data presentation,
- Example of implementation with R.

Not the focus of this lecture

- *Infographics*
- Cognitive aspect of data perception...

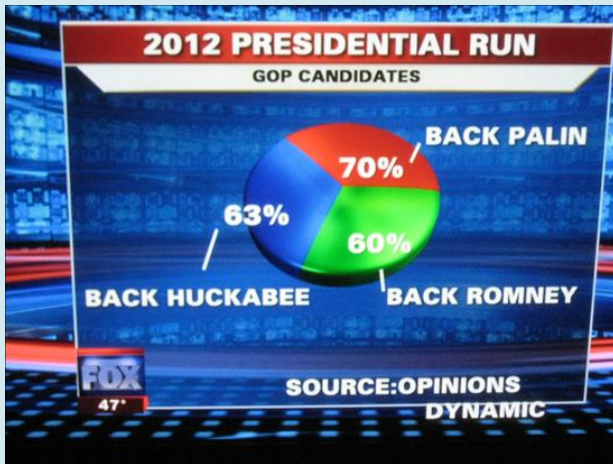
Goal

- Exposure to various plotting techniques.
- Proof of concept with R.
- *Visualize* the power of appropriate data graphics techniques



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization**
 - Introduction
 - **Bad Examples**
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

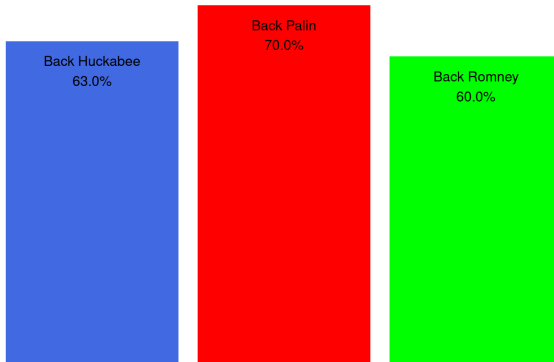
No Comment!



A possible fix

Bar Plot

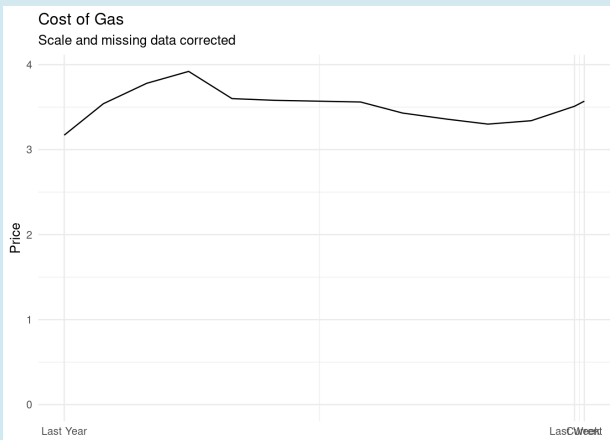
2012 Presidential Run



Scale Issue + Missing Data



Scale Issue Corrected + Missing Data Corrected



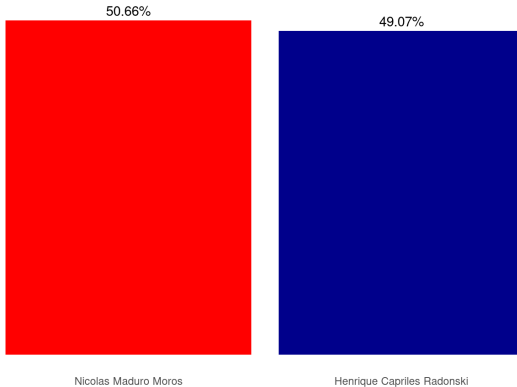
Truncated Axis Issue



Truncated Axis Issue Corrected

2013 Venezuelan presidential election

Truncated axis corrected





Scale Issue + Selection Issue

HOW 2012 STACKS UP

THE WARMEST YEARS ON RECORD
CONTIGUOUS U.S.

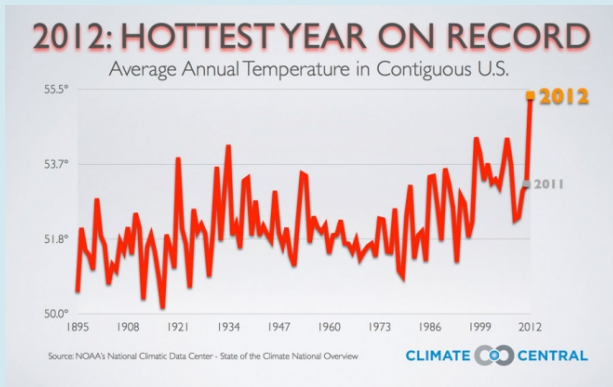


Source: NOAA's National Climatic Data Center - State of the Climate National Overview

CLIMATE  CENTRAL

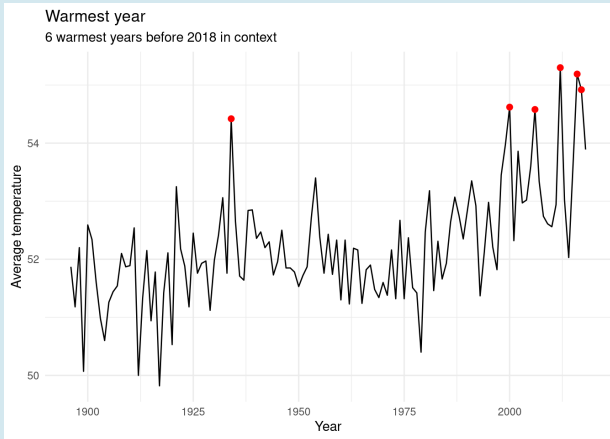


Scale Issue Corrected + Selection Issue Corrected



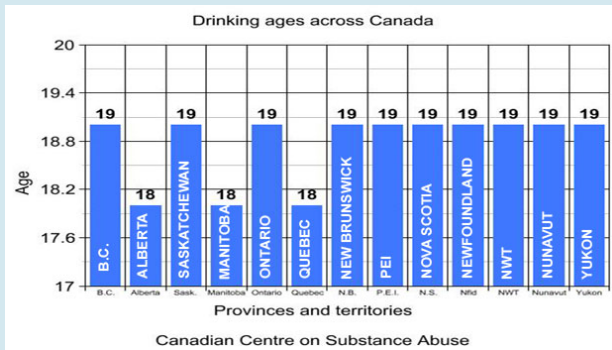


Scale Issue Corrected + Selection Issue Corrected (2018)





Truncated Axis + Clutter Issue



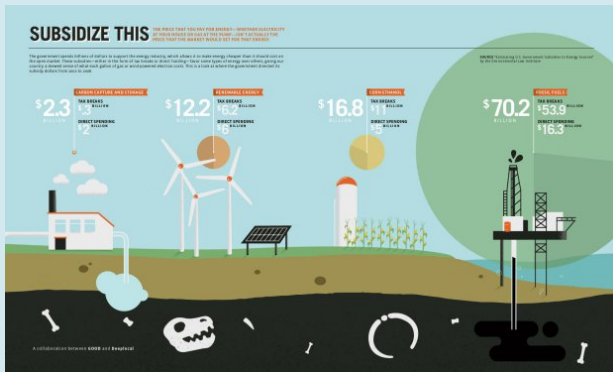


Truncated Axis + Clutter Issue Corrected?

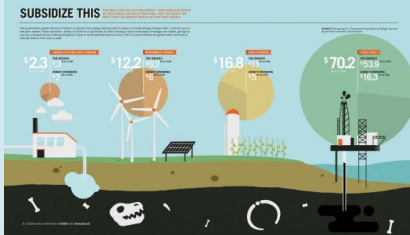
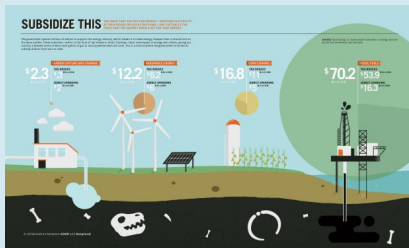
Drinking ages across Canada
Less clutter issue?

Alberta	18
Manitoba	18
Quebec	18
B.C.	19
Saskatchewan	19
Ontario	19
New Brunswick	19
PEI	19
Nova Scotia	19
Newfoundland	19
NWT	19
Nunavut	19
Yukon	19

Area Issue



Area Issue Corrected



Area Issue

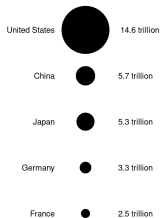


AMERICA'S ECONOMY 2010 GROSS DOMESTIC PRODUCT

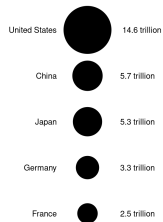


Area Issue Corrected

GDP 2012
Size issue



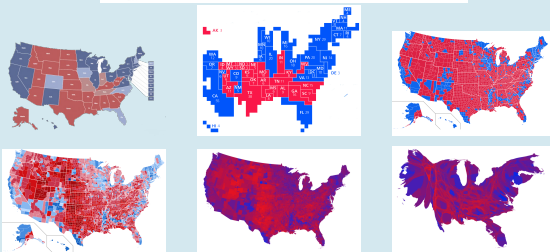
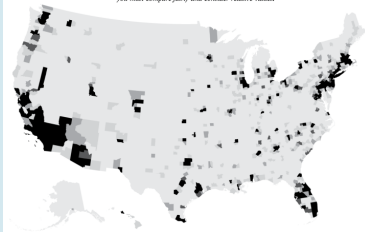
GDP 2012
Size issue corrected



Map Issue

SEEING ONLY IN ABSOLUTES

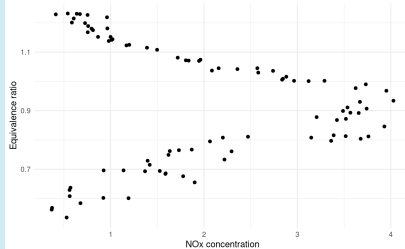
This is just population. When comparing across places, categories, or groups, you must compare fairly and consider relative values.



Unusual Axis Issue

A single-cylinder engine study of efficiency and exhaust emissions

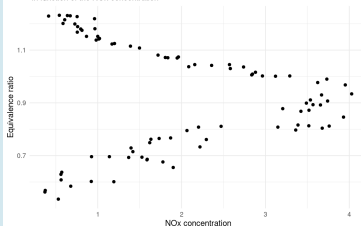
Equivalence ratio at which the engine was run (a measure of the richness of the air/ethanol mix) in function of the NO_x concentration



Unusual Axis Issue Corrected

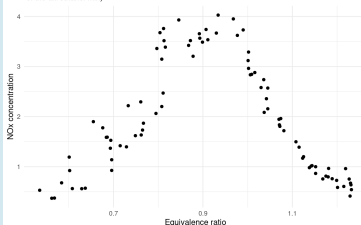
A single-cylinder engine study of efficiency and exhaust emissions

Equivalence ratio at which the engine was run (a measure of the richness of the air/ethanol mix) in function of the NOx concentration

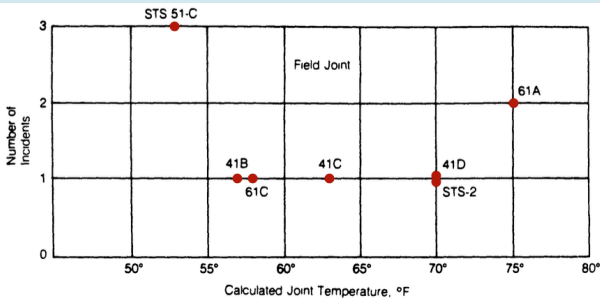


A single-cylinder engine study of efficiency and exhaust emissions

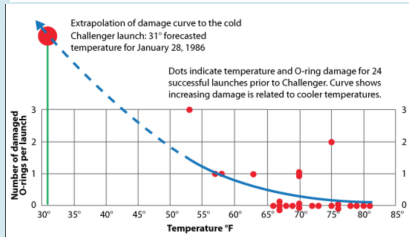
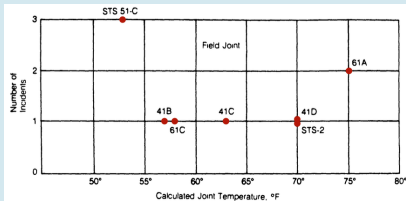
NOx concentration in function of the equivalence ratio at which the engine was run (a measure of the richness of the air/ethanol mix)



Catastrophic Issue



Catastrophic Issue Corrected



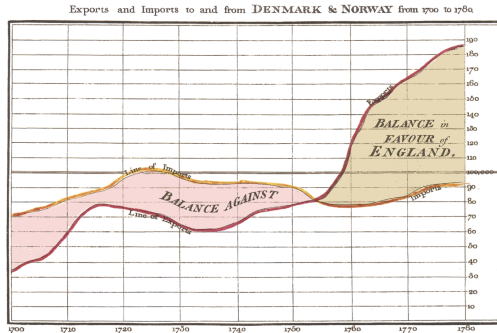
Outline



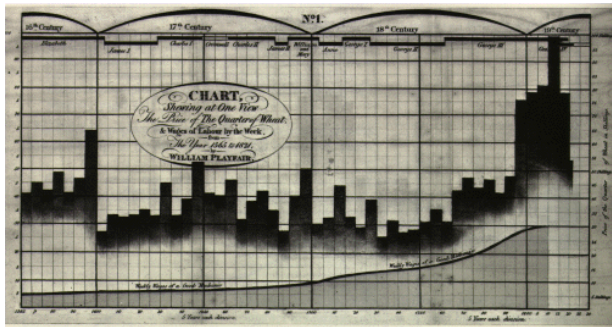
- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones**
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

William Playfair (1759-1823)

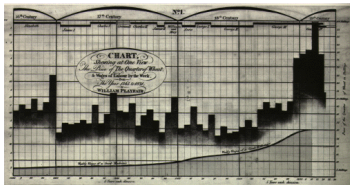
- Generally viewed as the inventor of most of the common graphical forms used to display data: line plots, bar chart and pie chart



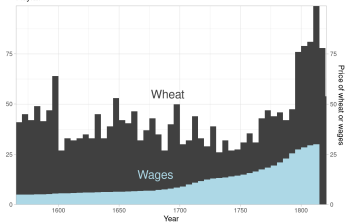
The Bottom line is divided into Years, the Right hand line into £10000 each.
Published in the Art Magazine, 1794, page 106, by W. Playfair. Plate page 302, 3rd ed., London.



- Unfortunately often flawed...

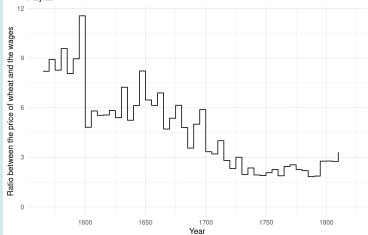


Evolution of the price of wheat and of the wages of a good mechanic
Playfair



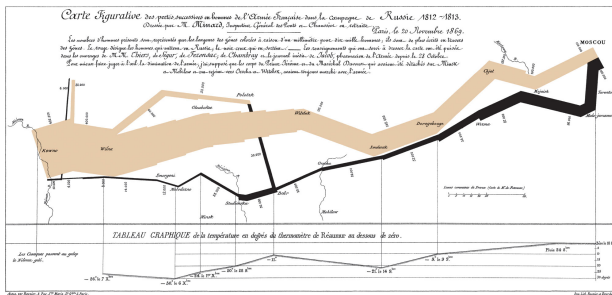
Issue Resolved?

Evolution of the price of Wheat and of the wages of a good mechanic
Playfair



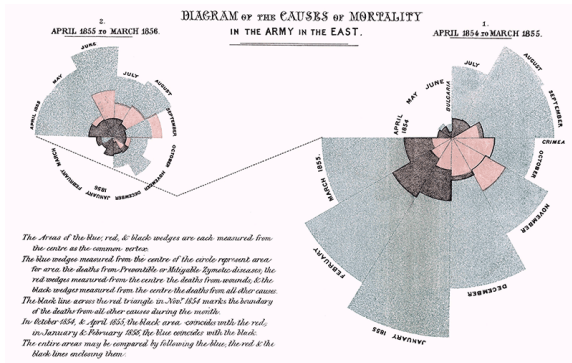
Charles Minard (1781-1870)

- contributed significantly in the field of information graphics in civil engineering and statistics and in particular in geographic maps.



Florence Nightingale (1820-1910)

- Mostly famous as a the mother of modern nursing. She also contributed to the use of graphical representation.

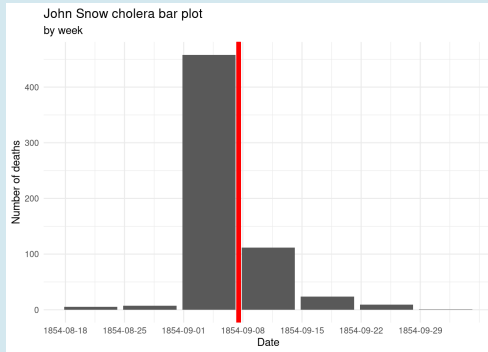


John Snow (1813-1858)

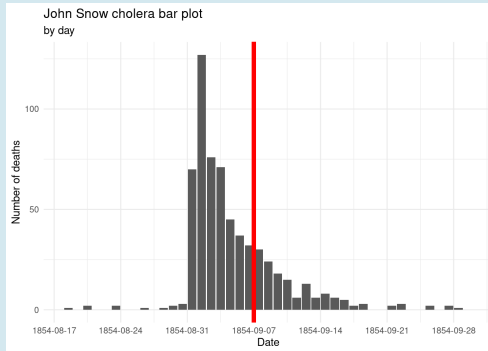
- An English physician famous for tracing the source of a cholera outbreak in London.

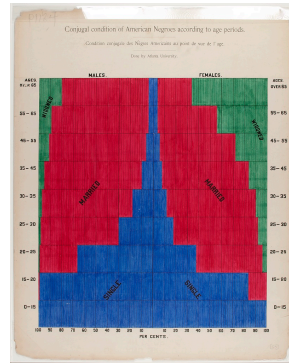
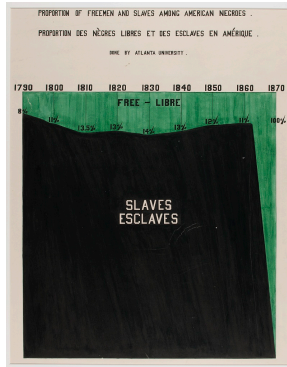


Story



Reality





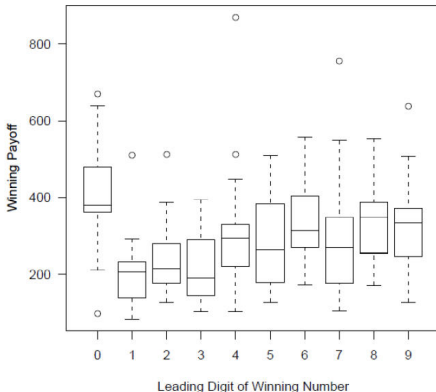
W. E. B. Du Bois (1868-1963)

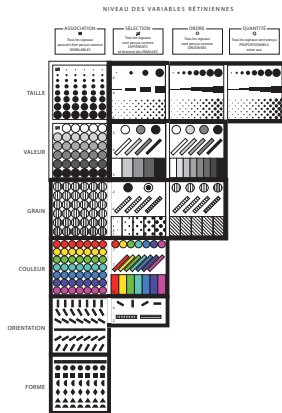
- African American activist and sociologist
- “Exhibit of American Negroes” organized to represent black contributions to the United States at the 1900 Exposition Universelle in Paris



Ronald Fisher (1890-1962) and John Tukey (1915-2000)

- Advance graphical methods for the analysis of data.
- Fisher: plot the data to understand relationships.
- Tukey promoted Exploratory Data Analysis!
- Tukey created the box plot and the stem and leaf plot.





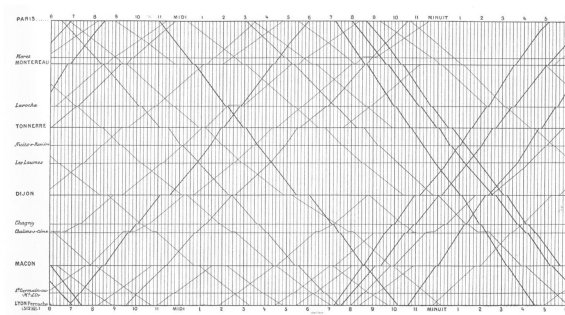
Jacques Bertin, "Sémiologie Graphique", 1973.

Jacques Bertin (1918-2010)

- *sémiologie graphique!*
- Systematic system of sign for information transmission.

Edward Tufte (1942-)

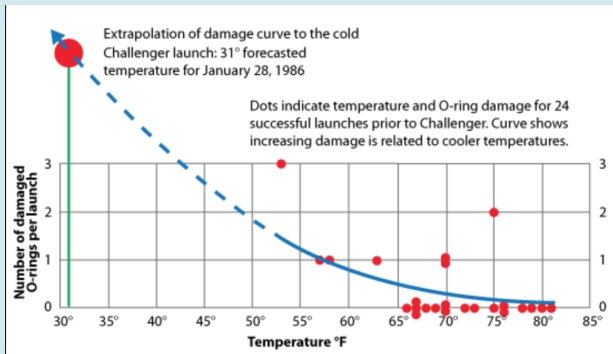
- Probably the most widely know works on data visualization.
- Highly compressed, elegant, and informative data, as expressed in dense printed graphics.
- Importance of *beauty* aspect...



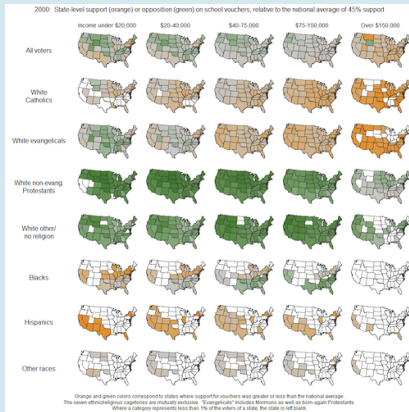
E.J. Marey (1885)

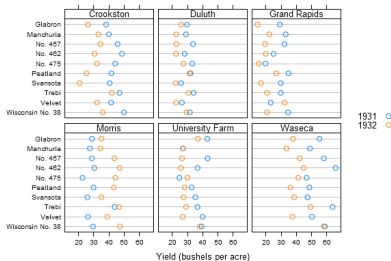


Challenger corrected!



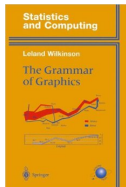
Small Multiples





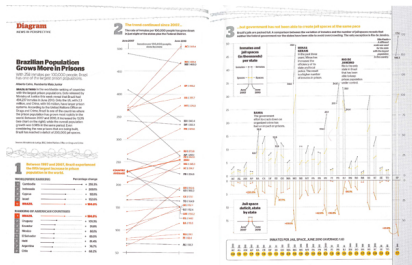
William Cleveland (1943-)

- His Elements of Graphing Data and Visualizing Data pioneered systematic considerations of legibility
- Cleveland is particularly known for promoting the dot plot as an alternative to bars and pies.
- The dot plot provides clarity and easy comparison of data.
- Cleveland also pioneered Trellis graphics that emphasizes comparison of multiple panels of data.



Leland Wilkinson (1945-)

- Its Grammar of Graphics was extremely influential in thinking about graphics:
 - Grammar means "rules for art and science"
 - Specifies rules both mathematical and aesthetic
 - Earlier graph producers focused on aesthetics of static content
 - Dynamic graphics and scientific visualization, by contrast, require sophisticated designs to enable brushing, drill-down, zooming, linking
 - The Grammar of Graphics is easily adapted to this approach
- `ggplot2` (Hadley Wickham) is inspired by this formalism!



Alberto Cairo

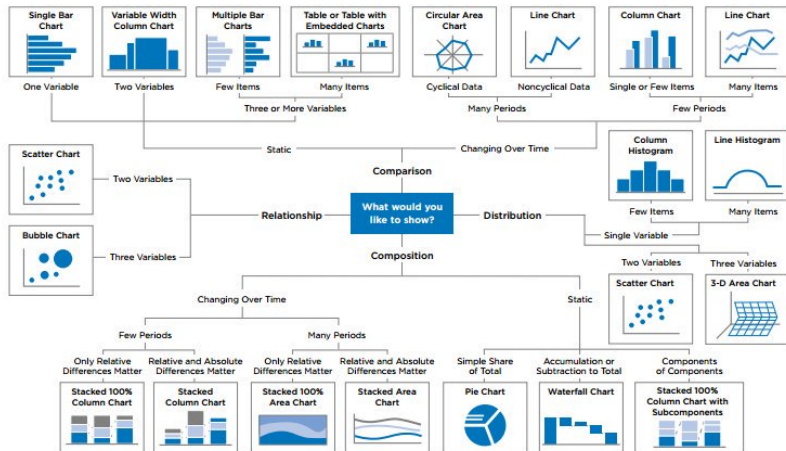
- Data Journalism / Importance of storytelling!
- *The functional art* : An introduction to Information Graphics and Visualization, the communication of facts and data by means of charts, graphs, maps, and diagrams.
- *The truthful art* : Explains how to transform elementary principles of data and scientific reasoning into tools that you can use in daily life to interpret data sets and extract stories from them.



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles**
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

How to Pick the Right Chart?

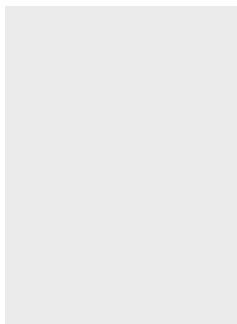
SELECTING THE APPROPRIATE CHART FOR STRATEGY PRESENTATIONS



How to Build a Graph?



cut	n
Ideal	21551
Premium	13791
Very Good	12082
Good	4906
Fair	1610

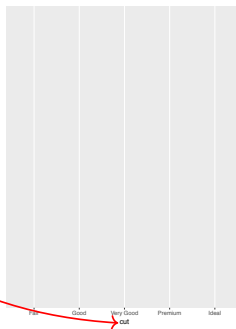


Bar Plot Example

- Start from the **data** and a blank canvas.

How to Build a Graph?

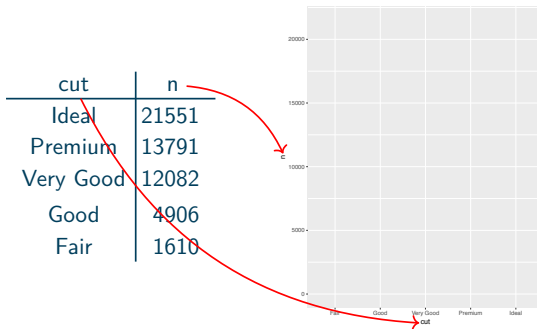
cut	n
Ideal	21551
Premium	13791
Very Good	12082
Good	4906
Fair	1610



Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.

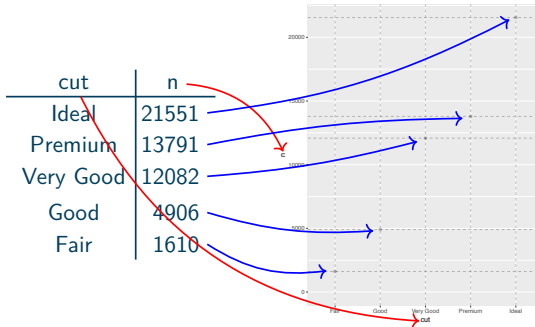
How to Build a Graph?



Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.

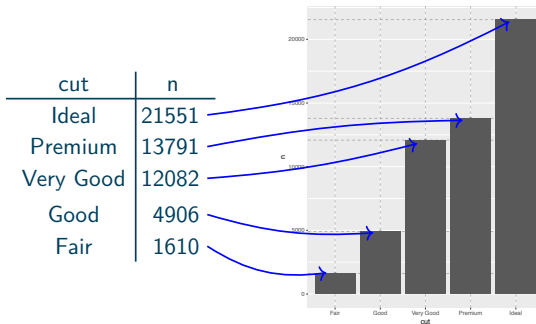
How to Build a Graph?



Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.

How to Build a Graph?

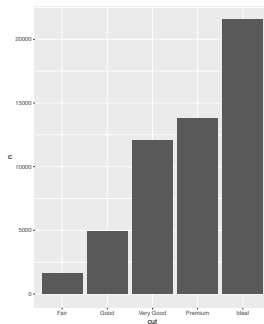


Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.
- Draw the graph with a certain **geometry**.

How to Build a Graph?

cut	n
Ideal	21551
Premium	13791
Very Good	12082
Good	4906
Fair	1610

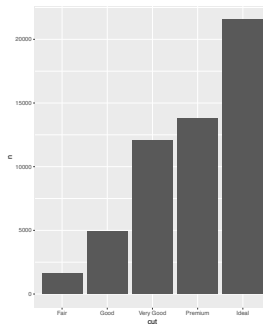


Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.
- Draw the graph with a certain **geometry**.

How to Build a Graph?

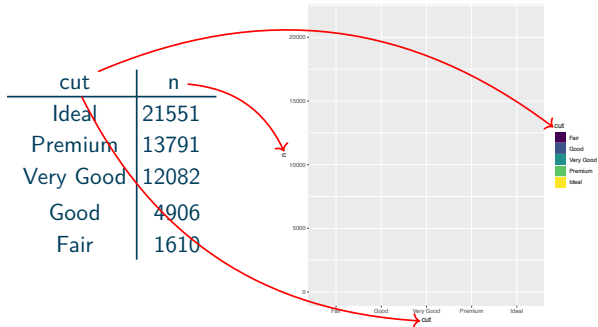
cut	n
Ideal	21551
Premium	13791
Very Good	12082
Good	4906
Fair	1610



Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.
- Draw the graph with a certain **geometry**.
- Systematic way of describing a graph.

How to Build a Graph?



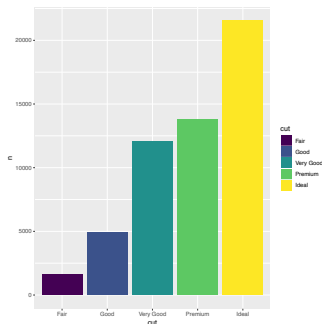
Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.
- Draw the graph with a certain **geometry**.
- Systematic way of describing a graph.

How to Build a Graph?



cut	n
Ideal	21551
Premium	13791
Very Good	12082
Good	4906
Fair	1610

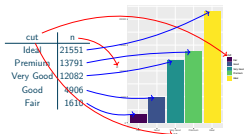


Bar Plot Example

- Start from the **data** and a blank canvas.
- Map **variables** to **axis**.
- Place the data with a **meaningful** mapping.
- Draw the graph with a certain **geometry**.
- Systematic way of describing a graph.

Grammar of Graphics

Principles



Describes all the non-data ink
Plotting space for the data
Statistical models & summaries
Rows and columns of sub-plots
Shapes used to represent the data
Scales onto which data is mapped
The actual variables to be plotted

Theme
Coordinates
Statistics
Facets
Geometries
Aesthetics
Data

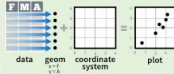


Wilkinson

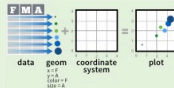
- **DATA** - weighting, reshaping, counting, bootstrapping
- **VARIABLES** - transform, sort, log, rank., resid., quant.
- **STATISTICS** - statistic preprocessing of data
- **AESTHETICS** - mapping between position/color/size/... and variable
- **SCALES** - nominal, ordinal, interval, ratio...
- **GEOMETRY** - line, area, etc., along with modifiers like jitter and dodge
- **COORDINATES** - refers to the coordinate system of the graph (cartesian, polar, etc.)
- **FACETS** - subgroups, multiway tables
- **GUIDES** - legends, axes, color scales, keys

ggplot2 cheatsheet

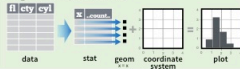
ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same few components: a **data** set, a set of **geoms**—visual marks that represent data points, and a **coordinate system**.



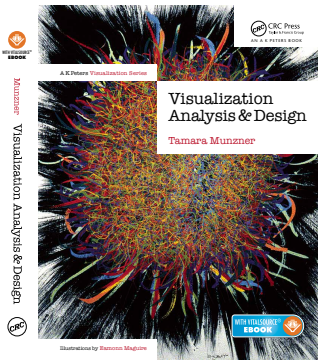
To display data values, map variables in the data set to aesthetic properties of the geom like **size**, **color**, and **x** and **y** locations.



Some plots visualize a **transformation** of the original data set. Use a **stat** to choose a common transformation to visualize, e.g. `a + geom_bar(stat = "bin")`



- ggplot2 (Hadley Wickham) is inspired by this formalism!



Visualization Analysis and Design

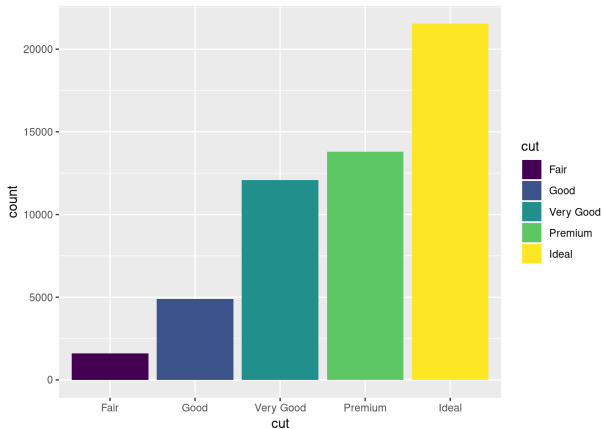
- Book from Tamara Munzner
- Published by CRC Press in 2014
- Supplementary slides *taken* from her slidedesk!



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

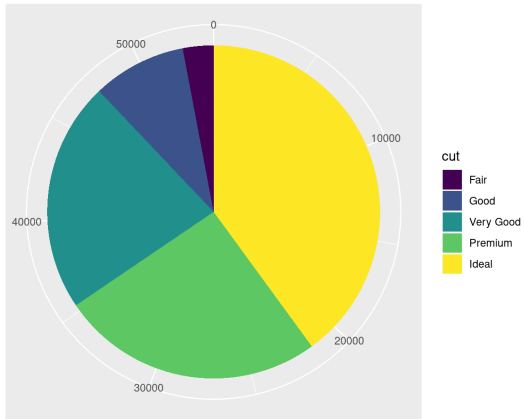


- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - **Univariate**
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle



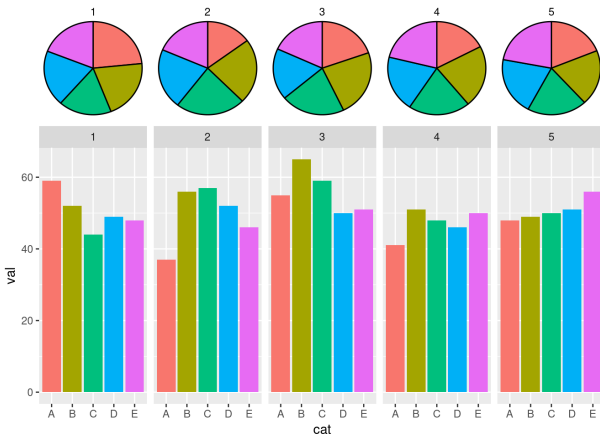
- Adapted to counts and quantities.

Proportion - Pie



- Should not be used for comparison...

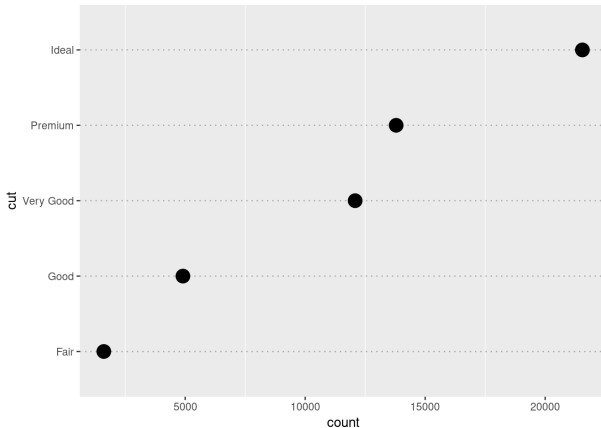
Proportion - Pie



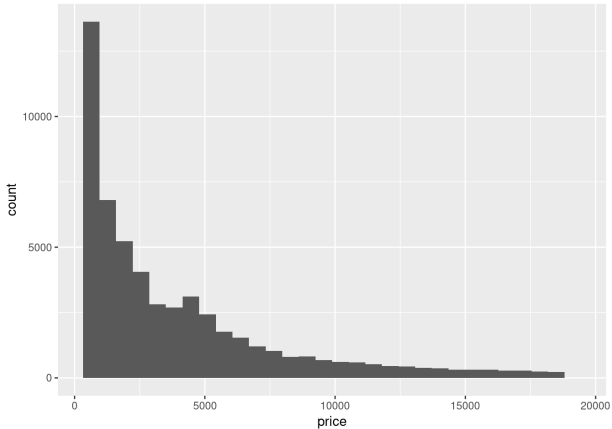
- Bar plots more efficient for comparison.
- Pie plots more efficient for global proportions!

Quantities - Cleveland Dot Plots

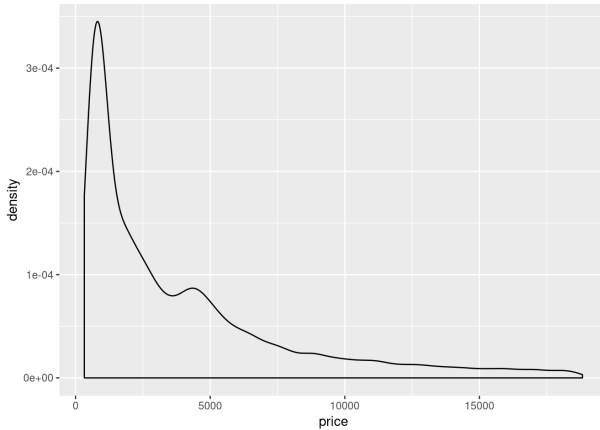
Classical Graphs



- Less *ink*, more pleasant...

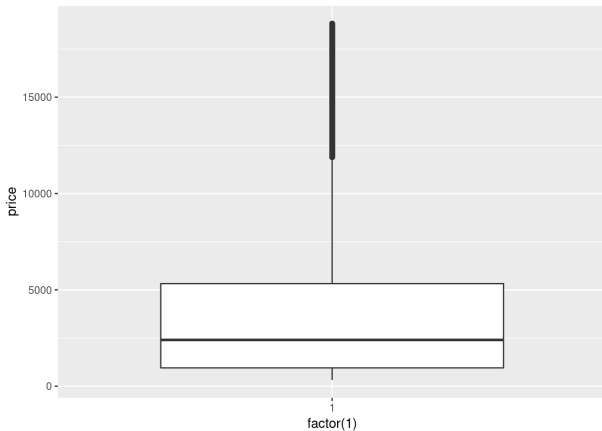


- Easily interpretable
- Adapted to continuous variable.



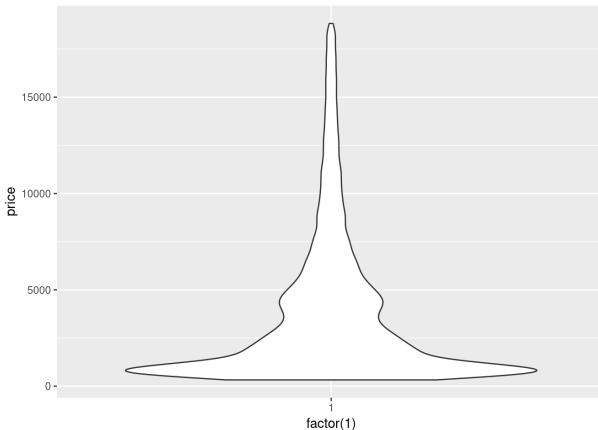
- Regularized view...

Distribution - Box and Whiskers



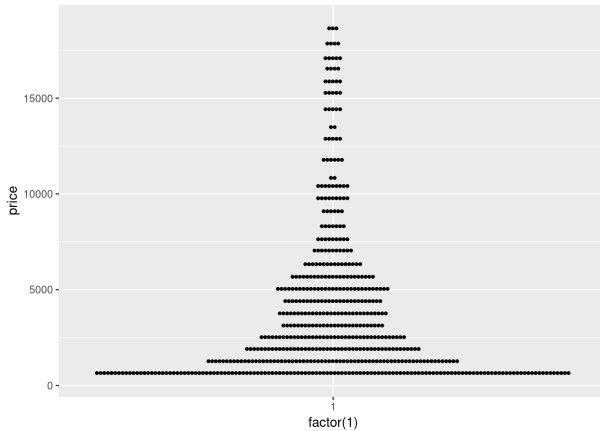
- Most classical representation after pie...

Distribution - Violin plot



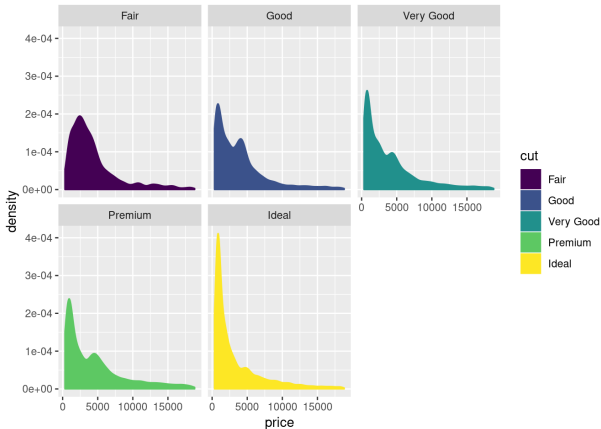
- Combined box plot and density estimation.

Distribution - Dot plots



- Combined binning and individuals...

Grouping

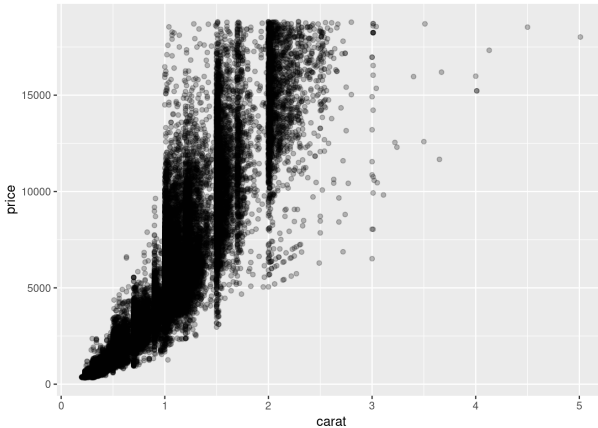


- Key to construct complex representation.



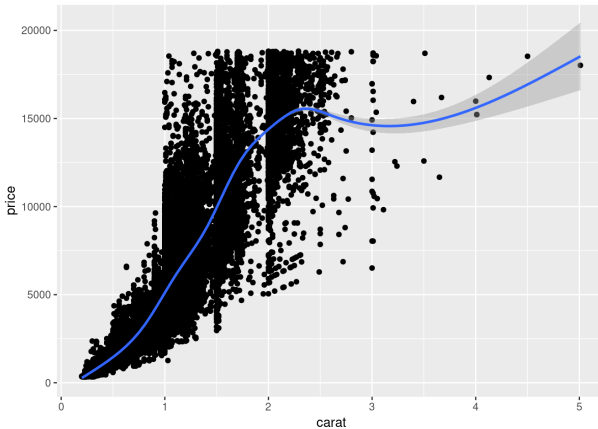
- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - Univariate
 - Multivariate**
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

Relation - Scatter Plot



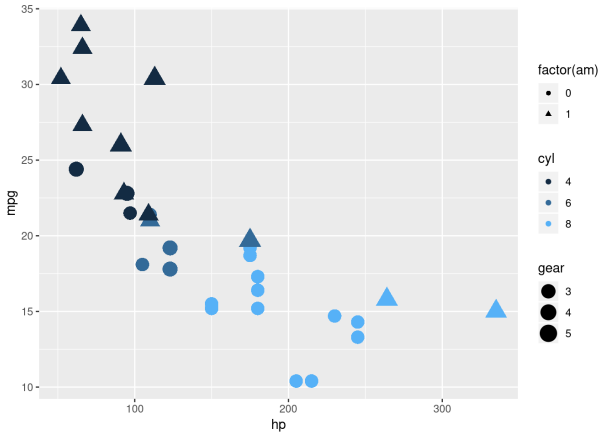
- Used to visualize the relationship between two variables.

Relation - Smoothing



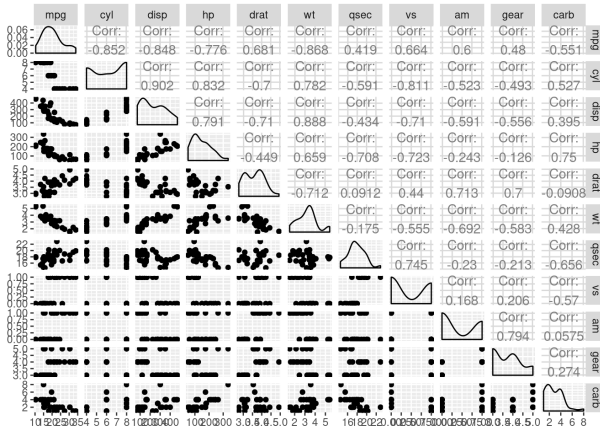
- Strong visual help.

Relation - Symbols



- Good idea to augment the information density...
- but can lead to too much complexity.

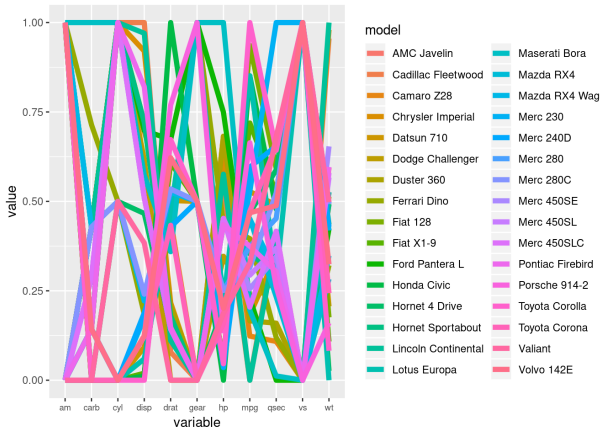
Grouping - Scatter Plot Matrix



- Gather all the dependencies...

HighD - Parallel Coordinates / Radar Plot

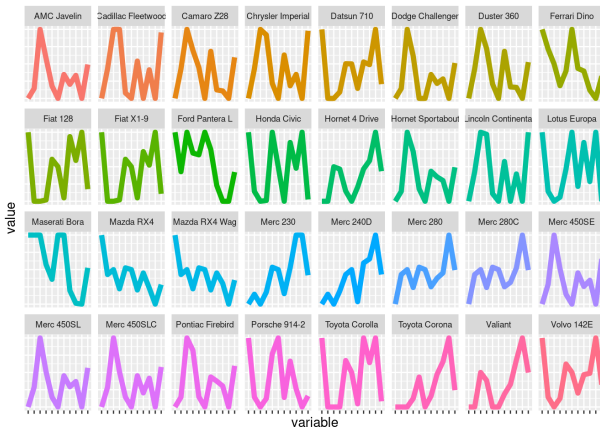
Classical Graphs



- Clever ideas to visualize groups.

HighD - Parallel Coordinates / Radar Plot

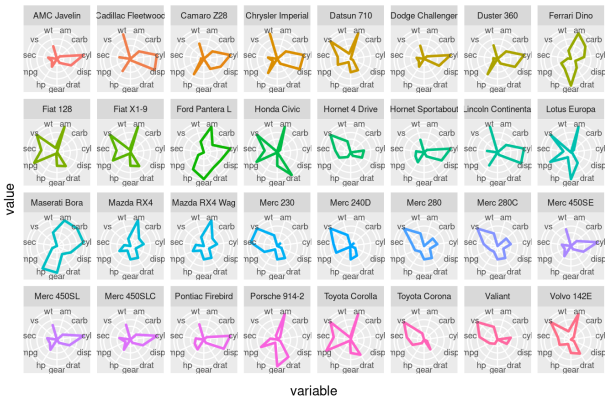
Classical Graphs



- Clever ideas to visualize groups.
- Example of small multiples

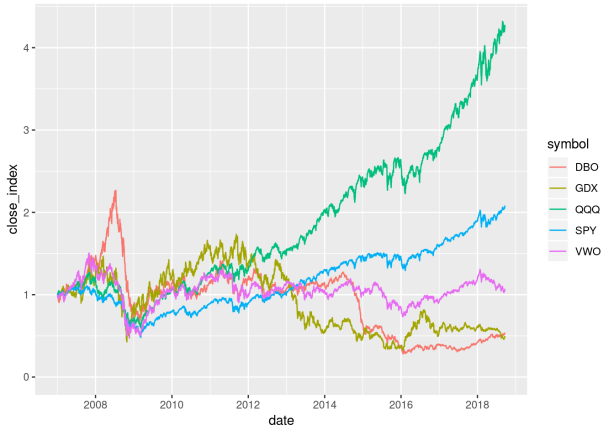
HighD - Parallel Coordinates / Radar Plot

Classical Graphs



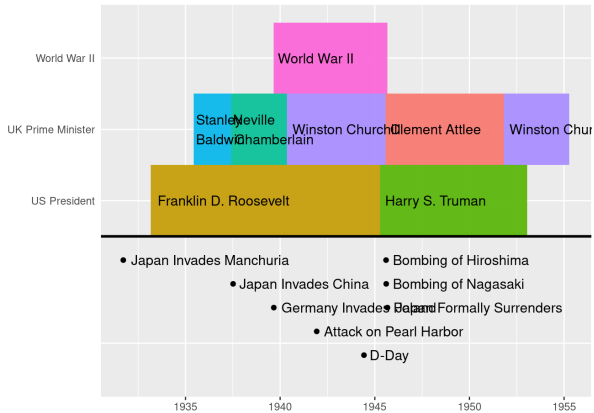
- Clever ideas to visualize groups.
- Example of small multiples

Evolution - Time series



- Order makes lines pertinent...
- Columns can also be used.

Evolution - Timeline

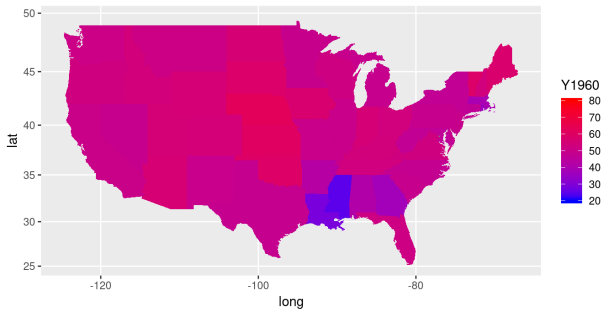


- Is this really a plot?



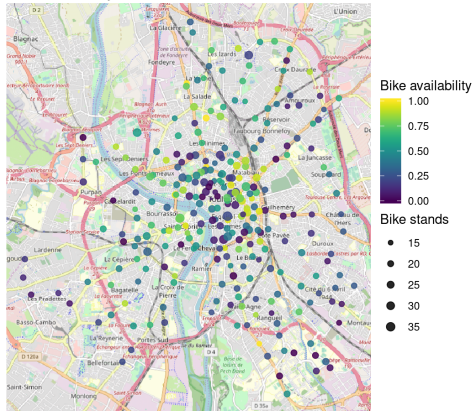
- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - Univariate
 - Multivariate
 - Maps**
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

Map - Choroplets

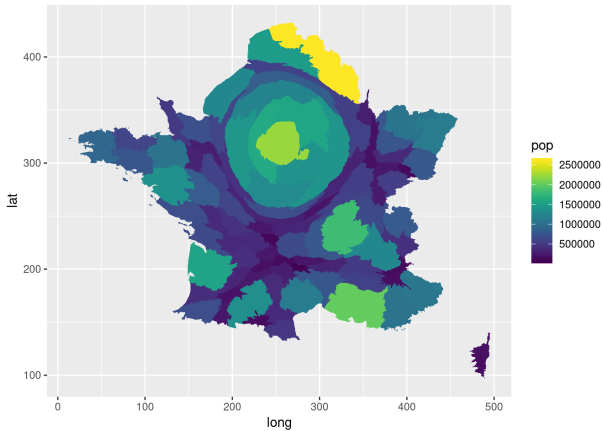


- Strong visual impact!

Bike availability

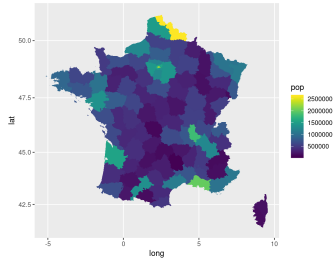
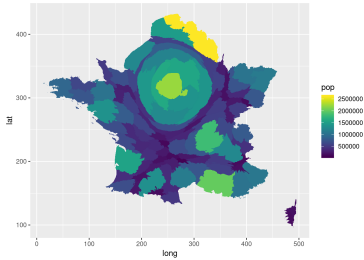


- Same ideas than decoration
- Could be extended to quite complex decorations...



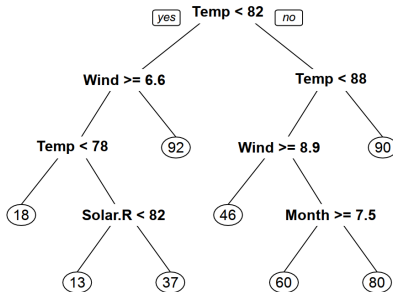
- Mainly useful when the reference is known.

Map - Cartograms



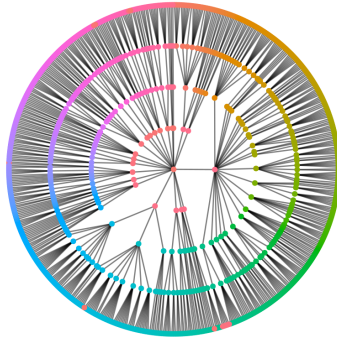


- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy**
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle



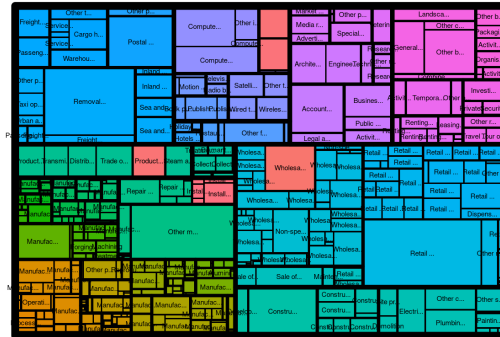
- Often use in classification...

Hierarchy - Tree Graph



- Polar variant.

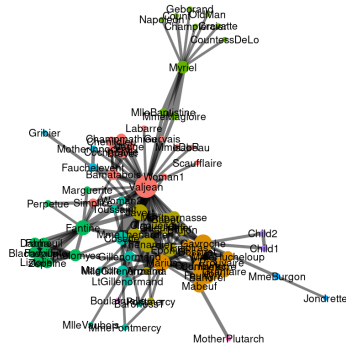
Hierarchy - Tree Map





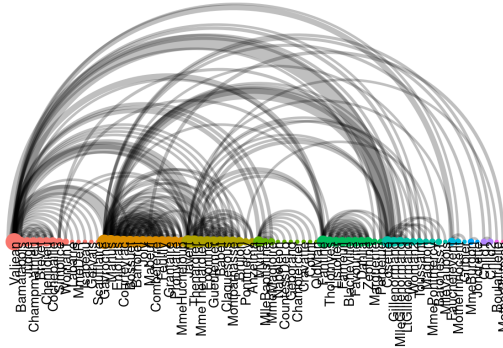
- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs**
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - **Networks**
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle

Network - Planar Layout

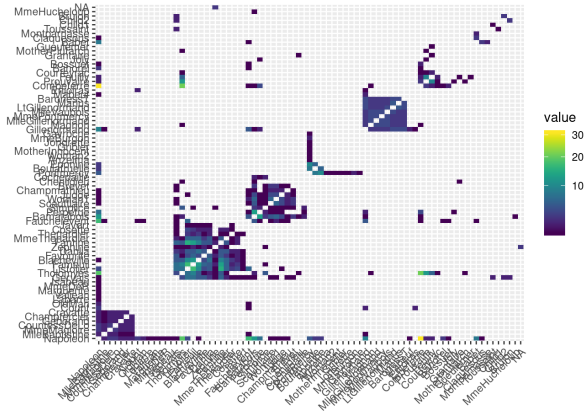


- Many possible layouts.

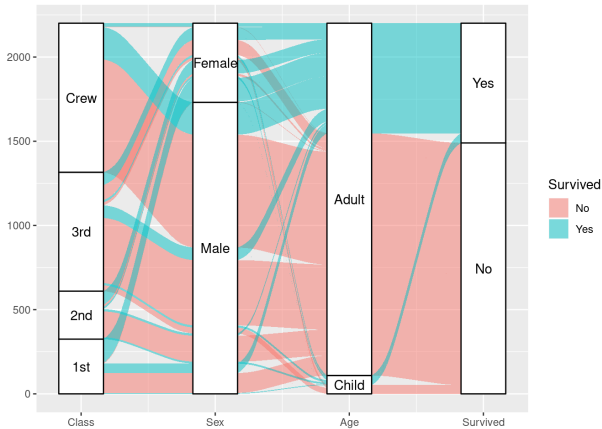
Network - Arc Diagram



- Very different layout...



- Adjacency matrix visualization.

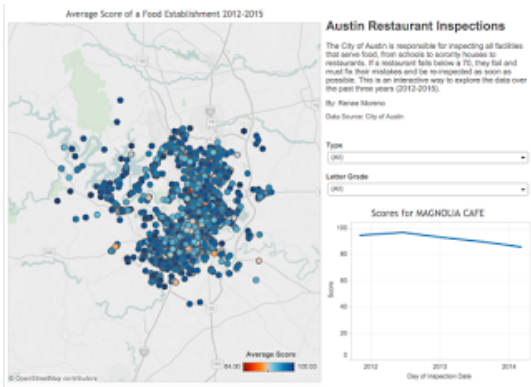


- Vertice oriented visualization.

Outline



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display**
- 8 Big Data
- 9 References
- 10 Miscellaneous
 - Visualization Principle



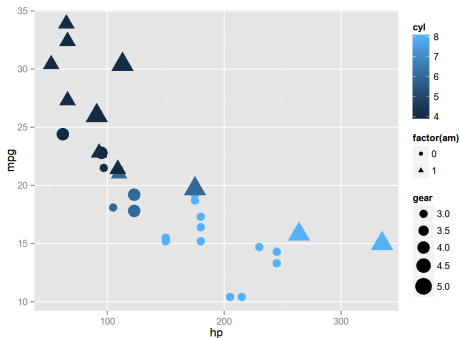
From static to dynamic

- Technology evolution: from paper to screen/mouse.
- Two directions:
 - Animation: use of time.
 - Interactivity: user interaction.



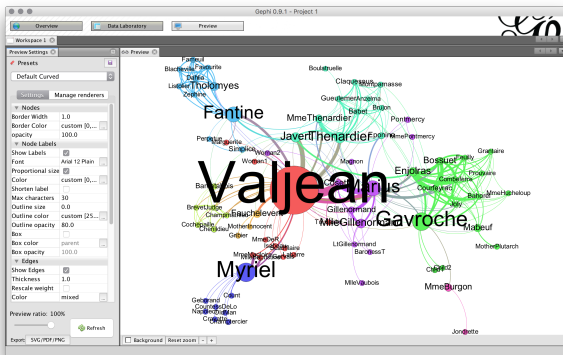
Animation

- Adapted to 1D mapping...
- Easily deployed (movie or animated picture)



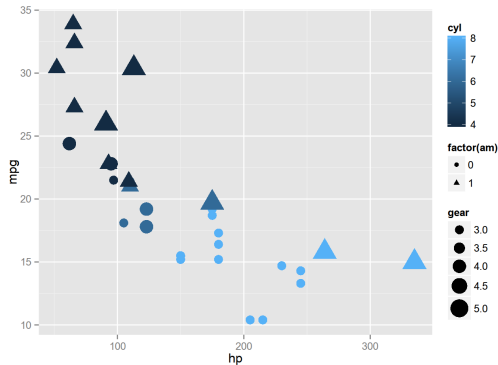
Interactivity: true dynamism

- More requirement.
- Solutions:
 - Standalone app (Gephi, Tulip...),
 - Javascript visualization libraries (d3.js, bokeh, plotly...)
 - Client/server infrastructure (Shiny, flask...)



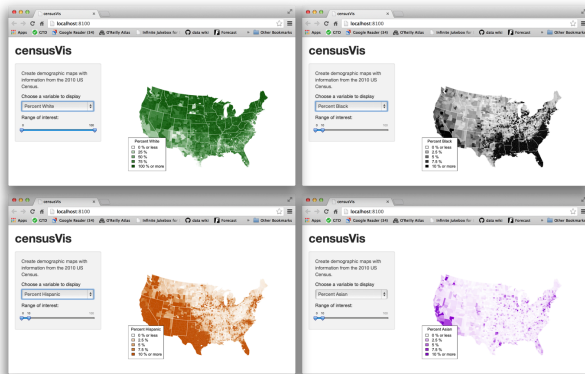
Dedicated software

- Gephi/Tulip for graphs
- Tableau
- ...



Javascript based frameworks

- Local (lightweight) computation.
- Examples:
 - Tooltip, Zoom, Brushing...
 - Linked panels...

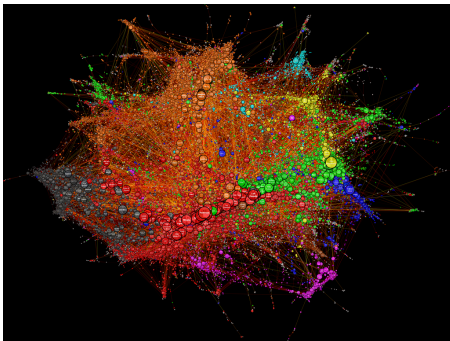


Client/Server Approach

- Shiny, Flask...
- Visualization on the client.
- Computation in the server.

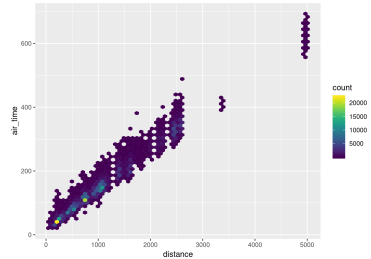
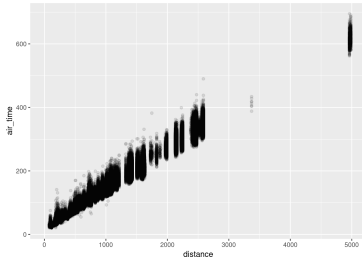


- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data**
- 9 References
- 10 Miscellaneous
 - Visualization Principle



More data points than pixels!

- Even if the processing possible, it is almost impossible to visualize faithfully the data!
- Summarization/selection required:
 - Grouping by categories or binning,
 - Small multiples,
 - Interactive selection.



- Binning \sim 2D histogram

Outline

References



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References**
- 10 Miscellaneous
 - Visualization Principle



L. Wilkinson.
The Grammar of Graphics.
Springer, 2011



H. Wickham.
ggplot2: Elegant Graphics for Data Analysis.
Springer, 2016



A. Cairo.
The Functional Art: An introduction to information graphics and visualization.
New Riders, 2012



A. Cairo.
The Truthful Art: data, charts and maps for communication.
New Riders, 2016



T. Munzner.
Visualization Analysis and Design.
CRC Press, 2014



K. Healy.
Data Visualization: A Practical Introduction.
Princeton University Press, 2018

Outline

Miscellaneous



- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous**
 - Visualization Principle

Outline

Miscellaneous

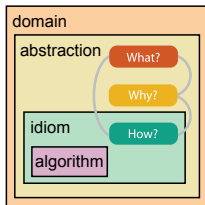


- 1 Introduction
- 2 Table Wrangling
- 3 Visualization
 - Introduction
 - Bad Examples
- 4 Historical Milestones
- 5 Principles
- 6 Classical Graphs
 - Univariate
 - Multivariate
 - Maps
 - Hierarchy
 - Networks
- 7 Interactivity and Dynamic Display
- 8 Big Data
- 9 References
- 10 Miscellaneous**
 - Visualization Principle

Nested model: Four levels of vis design

- *domain situation*
 - who are the target users?
- *abstraction*
 - translate from specifics of domain to vocabulary of vis
 - **what** is shown? **data** abstraction
 - **why** is the user looking at it? **task** abstraction
- *idiom*
 - **how** is it shown?
 - **visual encoding** idiom: how to draw
 - **interaction** idiom: how to manipulate
- *algorithm*
 - efficient computation

[A Nested Model of Visualization Design and Validation.
Munzner. *IEEE TVCG* 15(6):921-928, 2009
(*Proc. InfoVis 2009*).]



[A Multi-Level Typology of Abstract Visualization Tasks
Brehmer and Munzner. *IEEE TVCG* 19(12):2376-2385,
2013 (*Proc. InfoVis 2013*).]

Threats to validity differ at each level



What?

Why?

How?

What?

Datasets

→ Data Types

→ Items → Attributes → Links → Positions → Grids

→ Data and Dataset Types

Tables	Networks & Trees	Fields	Geometry	Clusters, Sets, Lists
Items	Items (nodes)	Grids	Items	Items
Attributes	Links	Positions	Positions	
	Attributes	Attributes		

→ Dataset Types

→ Tables



→ Multidimensional Table



→ Networks



→ Trees



→ Fields (Continuous)



→ Geometry (Spatial)



Attributes

→ Attribute Types

→ Categorical



→ Ordered

→ Ordinal



→ Quantitative



→ Ordering Direction

→ Sequential

→ Diverging



→ Cyclic



→ Dataset Availability

→ Static



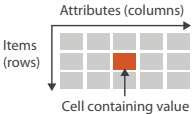
→ Dynamic



Three major datatypes

→ Dataset Types

→ Tables

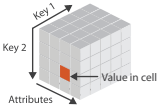


Attributes (columns)

Items (rows)

Cell containing value

→ *Multidimensional Table*



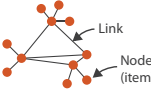
Key 1

Key 2

Attributes

Value in cell


→ Networks



Link

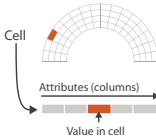
Node (item)

→ Trees



→ Spatial

→ Fields (Continuous)




Grid of positions

Cell

Attributes (columns)

Value in cell

→ Geometry (Spatial)



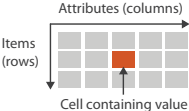
Position

- visualization vs computer graphics
– geometry is design decision

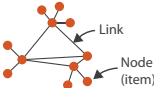
Types: Datasets and data

→ Dataset Types

→ Tables

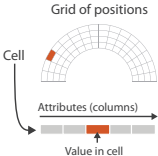


→ Networks



→ Spatial

→ Fields (Continuous)



→ Geometry (Spatial)



→ Attribute Types

→ Categorical



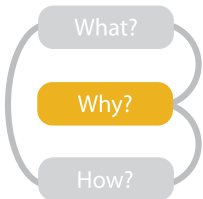
→ Ordered

→ Ordinal



→ Quantitative





- {action, target} pairs
 - discover distribution
 - compare trends
 - locate outliers
 - browse topology



Actions: Analyze, Query

- analyze

- consume

- discover vs present

- aka explore vs explain

- enjoy

- aka casual, social

- produce

- annotate, record, derive

- query

- how much data matters?

- one, some, all

- independent choices

→ Analyze

- Consume

- Discover



- Present



- Enjoy



- Produce

- Annotate



- Record



- Derive



→ Query

- Identify



- Compare



↑ ↓

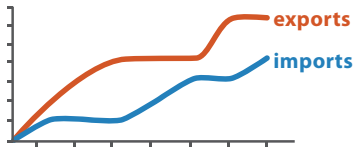


- Summarize

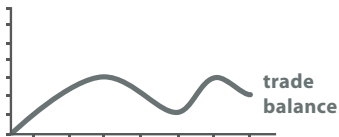


Derive: Crucial Design Choice

- don't just draw what you're given!
 - decide what the right thing to show is
 - create it with a series of transformations from the original dataset
 - draw that
- one of the four major strategies for handling complexity



Original Data



$$\text{trade balance} = \text{exports} - \text{imports}$$

Derived Data

Targets

→ All Data

→ Trends



→ Outliers



→ Features



→ Attributes

→ One

→ Distribution



→ Extremes



→ Many

→ Dependency



→ Correlation



→ Similarity



→ Network Data

→ Topology



→ Paths



→ Spatial Data

→ Shape



How?

Encode

→ Arrange

→ Express



→ Separate



→ Order



→ Align



→ Use



→ Map

from **categorical** and **ordered** attributes

→ Color

→ Hue



→ Saturation



→ Luminance



→ Size, Angle, Curvature, ...



→ Shape



→ Motion

Direction, Rate, Frequency, ...



Manipulate

→ Change



→ Select



→ Navigate



Facet

→ Juxtapose



→ Partition



→ Superimpose



Reduce

→ Filter



→ Aggregate



→ Embed



What?

Why?

How?

How to encode: Arrange space, map channels

Encode

① Arrange

→ Express



→ Order



→ Use



→ Separate



→ Align



② Map

from **categorical** and **ordered** attributes

→ Color

→ Hue



→ Saturation



→ Luminance



→ Size, Angle, Curvature, ...



→ Shape



→ Motion

Direction, Rate, Frequency, ...



Definitions: Marks and channels

- marks

 - geometric primitives

→ Points



→ Lines



→ Areas



- channels

 - control appearance of marks

→ Position

→ Horizontal



→ Vertical



→ Both



→ Color



→ Shape



→ Tilt



→ Size

→ Length



→ Area

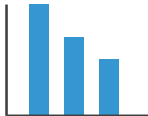


→ Volume



Encoding visually with marks and channels

- analyze idiom structure
 - as combination of marks and channels



1:
vertical position

mark: line



2:
vertical position
horizontal position

mark: point



3:
vertical position
horizontal position
color hue

mark: point

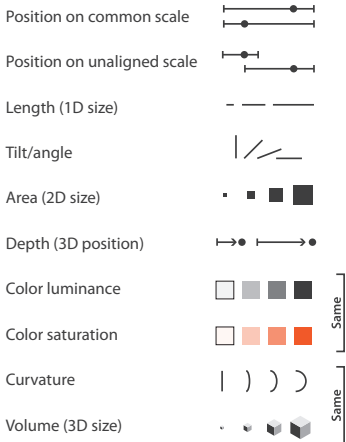


4:
vertical position
horizontal position
color hue
size (area)

mark: point

Channels: Rankings

➔ Magnitude Channels: Ordered Attributes



➔ Identity Channels: Categorical Attributes



- **expressiveness principle**
 - match channel and data characteristics
- **effectiveness principle**
 - encode most important attributes with highest ranked channels

Four strategies to handle complexity

→ *Derive*



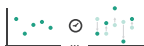
- derive new data to show within view
- change view over time
- facet across multiple views
- reduce items/attributes within single view

more at:

Visualization Analysis and Design.
Munzner. AK Peters Visualization Series, CRC Press, 2014.

Manipulate

→ Change



→ Select

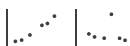


→ Navigate



Facet

→ Juxtapose



→ Partition



→ Superimpose



Reduce

→ Filter



→ Aggregate



→ Embed



What?

Datasets

Attributes

Data Types

→ Items

Why?

👉 Actions

🎯 Targets

Data and D

Tables

Items

Attributes

Analyze

→ Consume

→ Discover

→ Present

→ Enjoy



All Data

→ Trends

→ Outliers

→ Features



Dataset Typ

→ Tables

→ Produce

→ Annotate



Encode

How?

Manipulate

Facet

Reduce

Arrange

→ Express

→ Separate



→ Order

→ Align



→ Use



Map

from **categorical** and **ordered** attributes

→ Color

→ Hue → Saturation → Luminance



→ Size, Angle, Curvature, ...



→ Shape



→ Motion

Direction, Rate, Frequency, ...



Change



Select



Navigate



Juxtapose



Partition



Superimpose



Filter



Aggregate



Embed



Search

→ Multidim



key

Attributes

	Attr	
Location known	.	.
Location unknown	<	>

Query

→ Identify



What?

Why?

domain

abstraction

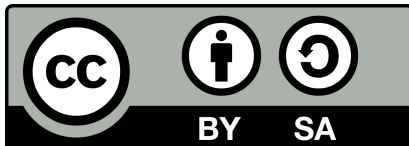
What?

Why?

idiom

How?

algorithm



Creative Commons Attribution-ShareAlike (CC BY-SA 4.0)

- You are free to:
 - **Share:** copy and redistribute the material in any medium or format
 - **Adapt:** remix, transform, and build upon the material for any purpose, even commercially.
- Under the following terms:
 - **Attribution:** You must give appropriate credit, provide a link to the license, and indicate if changes were made. You may do so in any reasonable manner, but not in any way that suggests the licensor endorses you or your use.
 - **ShareAlike:** If you remix, transform, or build upon the material, you must distribute your contributions under the same license as the original.
 - **No additional restrictions:** You may not apply legal terms or technological measures that legally restrict others from doing anything the license permits.

Contributors

- S. Boucheron, A.K. Fermin, S. Gaiffas, A. Guilloux, Ch. Keribin, E. Le Penec, E. Matzner, E. Scornet and X Exed team.